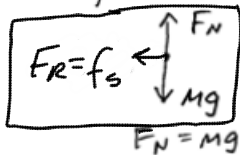


$F_N$  is what person feels he weighs,  
 use  $\vec{\Sigma F} = M\vec{a}_R$  Radial (or Centripetal) Force

1) Car turning on flat road.



$$\Sigma F_R = \frac{MV^2}{r} \quad \mu_s F_N = \frac{MV^2}{r} \quad V^2 = \mu_s g r$$

$$f_s = \frac{MV^2}{r} \rightarrow \mu_s Mg = \frac{MV^2}{r} \rightarrow V = \sqrt{\mu_s g r}$$

2) Car turning on banked track so there is no tendency to slide up or down the track. In this case, no friction is needed.



$$F_N > Mg$$

$$\Sigma F_y = 0 \quad \Sigma F_R = \frac{MV^2}{r} \quad \tan \theta = \frac{V^2}{gr}$$

$$F_N \cos \theta - Mg = 0 \quad F_R = \frac{MV^2}{r} \quad V^2 = gr \tan \theta$$

$$F_N \cos \theta = Mg \quad F_N \sin \theta = \frac{MV^2}{r} \quad V = \sqrt{gr \tan \theta}$$

$$F_N = \frac{Mg}{\cos \theta} \quad \frac{Mg}{\cos \theta} \sin \theta = \frac{MV^2}{r}$$

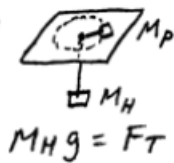
$F$  is apparent weight.

3) Conical pendulum. Exactly the same as car on banked track, except  $F_N$  becomes  $F_T$  in string.  $\theta$  is angle string makes with the vertical.



4) Plane banking while turning. Exactly the same as car on banked track and conical pendulum, except  $F_N$  is either the normal force on a passenger or it becomes  $F_L$ , the lift provided by the wing.

5) Puck rotating on frictionless table. Hanging mass provide  $F_c$ .



$$M_h g = F_T$$

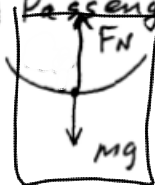
$$\Sigma F = \frac{M_p V^2}{r} \quad M_h g = \frac{M_p V^2}{r}$$

$$F_T = \frac{M_p V^2}{r} \quad V^2 = \frac{M_h g r}{M_p}$$

This is problem 25

or

6) Passenger in roller coaster going through a dip. Car, also.



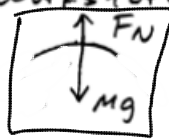
$$F_N = \frac{MV^2}{r} + Mg$$

$$F_R = F_N - Mg \quad F_N = M \left( \frac{V^2}{r} + g \right)$$

$F_N$  is apparent weight. Rider feels heavier because  $F_N > Mg$ . This causes car and rider to go up.  $F_N$  is what rider feels he weighs.

7) Passenger in roller coaster going over the top of a hill.

Works for car, too.



$$\sum \vec{F} = m\vec{a}_R$$

$$F_R = Mg - F_N$$

$$F_R = Mg - F_c$$

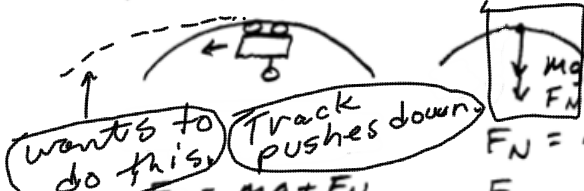
$$F_N = Mg - \frac{Mv^2}{r}$$

$$F_N = M(g - \frac{v^2}{r})$$

$F_N$  is apparent weight, Rider feels lighter because  $F_N < Mg$ . This causes car and rider to go down.

8) Passenger in roller coaster going inside loop at the top.

Car is going fast enough so rider won't fall out.



$$F_R = Mg + F_N$$

$$F_N = F_R - Mg$$

$$F_N = \frac{Mv^2}{r} - Mg$$

$$F_N = M(\frac{v^2}{r} - g)$$

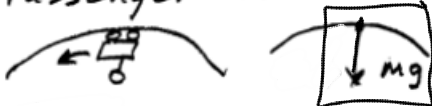
Rider feels a bit lighter than  $Mg$  in the diagram.

$F_N < Mg$  here.

$F_N$  is apparent weight but rider feels his weight points up!

9) Passenger in roller coaster going inside loop at the top,

Car is going just fast enough so rider won't fall out.



$$F_R = F_g$$

$$\frac{Mv^2}{r} = Mg$$

$$v^2 = gr$$

$$v = \sqrt{gr}$$

The normal force is zero! The weight is the  $F_R$ .

10) Passenger in roller coaster going inside loop at the top,

Car is going too slow,  $Mg > F_R$ .

Rider will fall out without seat belt or bar,  $F_N$  pulls rider up

$$F_R = Mg - F_N$$

$$F_N = Mg - F_R$$

$F_N$  is apparent weight. Rider feels his weight down but less than  $Mg$  in this diagram.

$$F_N = Mg - \frac{Mv^2}{r}$$

$$F_N = M(g - \frac{v^2}{r})$$

Rider wants to go in a parabola smaller than the track, Seat belt keeps him up.

