

Honors Physics Quiz - Energy Conservation - Ch. 5

$$K_i + U_i = K_f + U_f \quad K = \frac{1}{2}mv^2 \quad U = mgh \quad P = W/t$$

1. Mr. Bean falls asleep on a roller coaster. When he wakes up, he is 10 m above ground and going uphill. When he goes over the next hill, which is 45 m above ground, he is going 14.5 m/s. How fast was he going when he woke up at the 10 m mark if all forces are conservative?

$$K_i + U_i = K_f + U_f$$

$$\frac{1}{2}mv_i^2 + mgh_i = \frac{1}{2}mv_f^2 + mgh_f$$

$$v_i^2 + 2gh_i = v_f^2 + 2gh_f$$

$$v_i^2 = v_f^2 + 2gh_f - 2gh_i$$

$$v_i = \sqrt{v_f^2 + 2g(h_f - h_i)}$$

$$= \sqrt{(14.5 \frac{m}{s})^2 + 2(9.8 \frac{m}{s^2})(45m - 10m)}$$

$$\boxed{v_i = 29.9 \frac{m}{s}}$$

$$h_i = 10m$$

$$h_f = 45m$$

$$v_f = 14.5 \frac{m}{s}$$

$$v_i = \frac{m}{s}$$

2. If, instead, Mr. Bean ran up stairs that were 35 m high in 125 seconds, what is his power in watts if his mass is 80 kg?

$$P = \frac{W}{t}$$

$$= \frac{mgh}{t}$$

$$= \frac{80kg(9.8 \frac{m}{s^2})(35m)}{125s}$$

$$\boxed{P = 220 W}$$

EC - If instead, in question 1, Mr. Bean went over the hill at 8.0 m/s, how much energy was lost due to friction?

$$K_i + U_i + E_{in} - E_{out} = K_f + U_f$$

$$\frac{1}{2}mv_i^2 + mgh_i + 0 - E_{out} = \frac{1}{2}mv_f^2 + mgh_f$$

$$-E_{lost} = \frac{1}{2}m(v_f^2 - v_i^2) + mg(h_f - h_i)$$

$$= \frac{1}{2}(80kg) \left[(8 \frac{m}{s})^2 - (29.9 \frac{m}{s})^2 \right] + 80kg(9.8 \frac{m}{s^2})(45m - 10m)$$

$$\boxed{E_{lost} = 5760 J}$$